# Research of techniques to improve the performance of explicit numerical methods on the CPU

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# Introducing

- Explicit numerical methods are used for a wide range of scientific problems
- Need to speed up stencils calculation
- SIMD-computing
- Tiling (recursive and non-recursive)

# Introducing

- Explicit numerical method -the solution of the acoustic equation in three dimensional space by the FDTD
- Six-core CPU Intel (R) Xeon (R) E5-2620 v2 (2.1 GHz) 32 KB (L1), 256 KB (L2), 15 MB (L3)
- GCC 8.1.0 with OpenMP

•  $N = \frac{N_x * N_y * N_z * N_t * Op}{T_{calc} * Freq_{cpu} * k * M_{kernel}}$  – the percentage of peak performance



### Vectorization

- Perform the same operation (addition or multiplication) with several data simultaneously
- AVX-instructions ( $_m256d$  register) with 4 double values
- Used vectorization for external spatial cycle



Stencil representation in vectors with shifts

# Cube tiling (non-recursive)

- Need to traverse  $N_x * N_y * N_z * N_t$
- Tile size fixed



Tile representation in XT

Y						
4	5	6	7	8	9	
3	4	5	6	7	8	
2	3	4	5	6	7	
1	2	3	4	5	6	X

Parallel tile calculation in XY

# Cube tiling (non-recursive)

• Gcells/s - number of nodes calculated per second



Graph of the number of points calculated per second from a fixed tile size on various threads

#### Cube tiling (non-recursive)



Graph of the number of threads on the speed up of calculations for cube-tiling

# Cube tiling (recursive)

•  $h = 2^{k-1}$  the distance between tiles at the current recursion level

			$ T \vee                                  $
Grid	GCell/	Tile	
Size	S	size	
$128^{4}$	0.284	64	
256^4	0.268	64	Recursive tile splitting in XYT
1024^4	0.189	64	
128^4	0.235	128	
256^4	0.263	128	• Best Gcell/s for non-recursive method is
1024^4	0.164	128	2.07 GCell/s
$256^{4}$	0.263	256	
1024^4	0.155	256	

#### Diamond-shape tiling (non-recursive)

• Turning cube tile for 45 degree



Diamond-shape tile



 $Tile\ parallel\ calculation$ 

# Diamond-shape tiling (non-recursive)

• Cache misses



Graph of the number of points calculated per second from a fixed tile size on various threads

#### Diamond-shape tiling (non-recursive)



The graph of the number of threads on the speedup of calculation for diamondshape tiling

# Diamond-shape tiling (recursive)

• Variation of recursion level



Graph of dependence of the number of points calculated per second from the recursion level of the iteration space in X recursive tile, size 128 on various threads

# Conclusion

- Non-local vectorization with cube tiling get best performance stencil calculation
- Recursive tiling doesn't improve performance



A plot of the number of threads on the efficiency of paralleling

Version of program	Percentage of peak computing performance
Origin	2.4 %
AutoVec	5.4~%
AlignedVec	5.9 %
CubeTiling	36.6 %
DiamTiling	28.7 %

# Thanks you for your attention !